

# Vorlesung

# Grundlagen der

# Künstlichen Intelligenz

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# Chapter 12

# Knowledge representation

# Outline

- Ontological engineering
- Categories and objects
- Actions, situations and events
- Mental events and mental objects
- The internet shopping world
- Reasoning systems for categories
- Reasoning with default information
- Truth maintenance systems

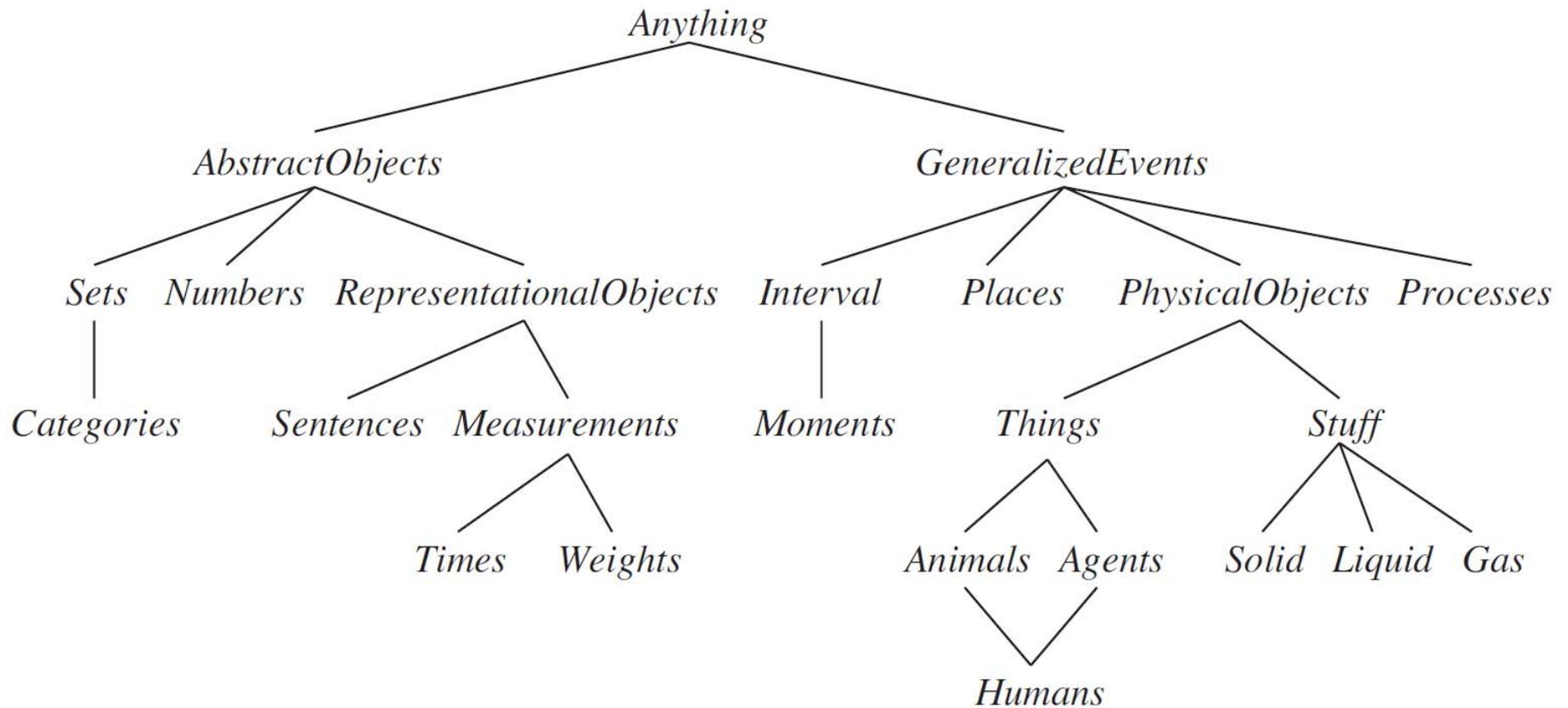


# Ontological engineering

- How to create more general and flexible representations.
  - Concepts like actions, time, physical object and beliefs
  - Operates on a bigger scale than K.E.
- Define general framework of concepts
  - Upper ontology
- Limitations of logic representation
  - Red, green and yellow tomatoes: exceptions and uncertainty



# The upper ontology of the world



January 7, 2013



# Difference with special-purpose ontologies

- A general-purpose ontology should be applicable in more or less any special-purpose domain.
  - Add domain-specific axioms
- In any sufficiently demanding domain different areas of knowledge need to be unified.
  - Reasoning and problem solving could involve several areas simultaneously
- What do we need to express?  
Categories, Measures, Composite objects, Time, Space, Change, Events, Processes, Physical Objects, Substances, Mental Objects, Beliefs



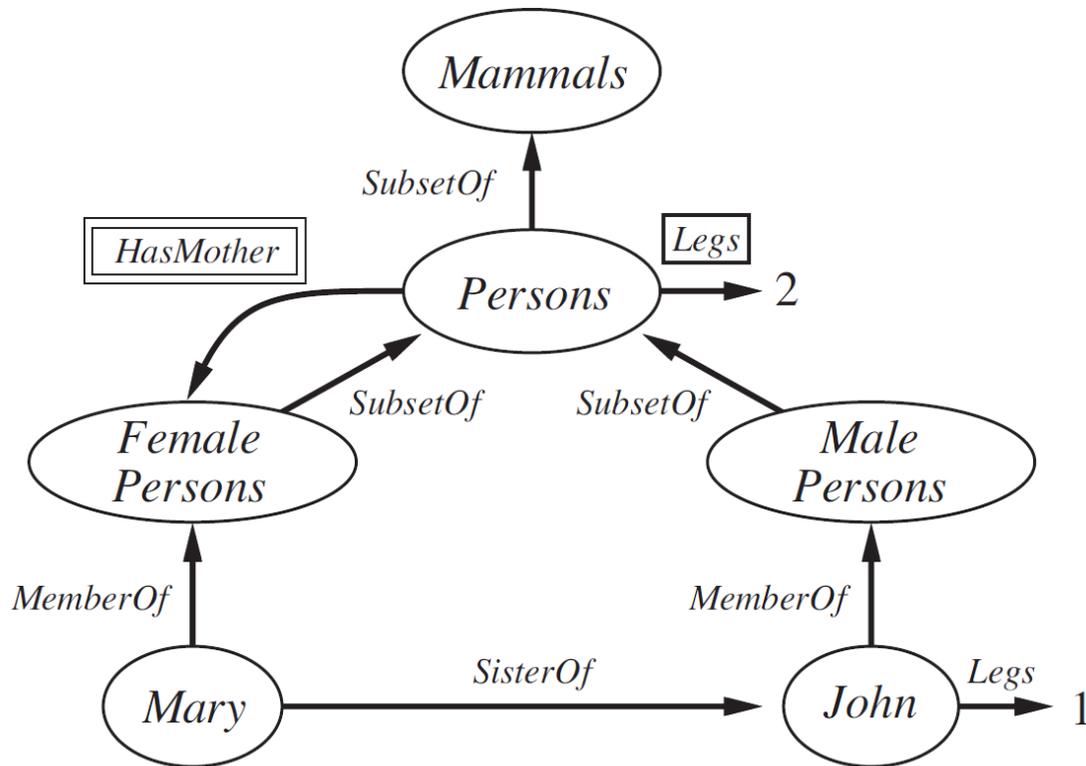
# Categories and objects

- KR requires the organisation of objects into categories
  - Interaction at the level of the object
  - Reasoning at the level of categories
- Categories play a role in predictions about objects
  - Based on perceived properties
- Categories can be represented in two ways by FOL
  - Predicates:  $\text{apple}(x)$
  - *Reification* of categories into objects: apples
- Category = set of its members



# Category organization

- Relation = *inheritance*:
  - All instance of food are edible, fruit is a subclass of food and apples is a subclass of fruit then an apple is edible.
- Defines a taxonomy

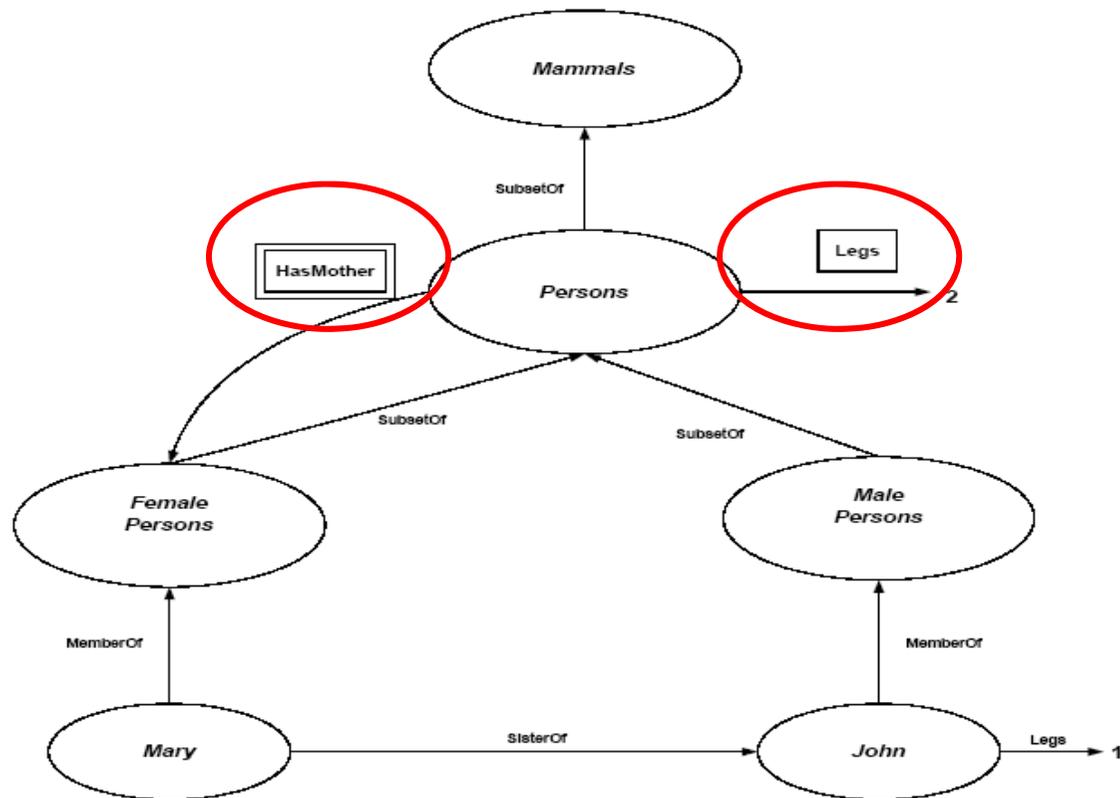


# Semantic Networks

- Logic vs. semantic networks
- Many variations
  - All represent individual objects, categories of objects and relationships among objects.
- Allows for inheritance reasoning
  - Female persons inherit all properties from person.
  - Cfr. OO programming.
- Inference of inverse links
  - SisterOf vs. HasSister



# Semantic network example

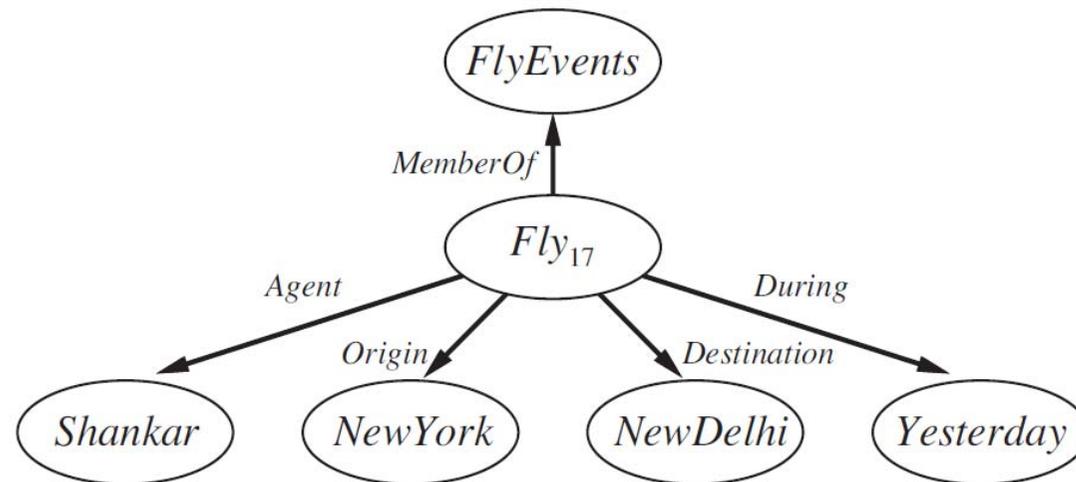


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# Semantic networks

- Drawbacks
  - Links can only assert binary relations
  - Can be resolved by reification of the proposition as an event



- Representation of default values
  - Enforced by the inheritance mechanism.



# FOL and categories

- An object is a member of a category
  - $\text{MemberOf}(\text{BB}_{12}, \text{Basketballs})$
- A category is a subclass of another category
  - $\text{SubsetOf}(\text{Basketballs}, \text{Balls})$
- All members of a category have some properties
  - $\forall x (\text{MemberOf}(x, \text{Basketballs}) \Rightarrow \text{Round}(x))$
- All members of a category can be recognized by some properties
  - $\forall x (\text{Orange}(x) \wedge \text{Round}(x) \wedge \text{Diameter}(x)=9.5\text{in} \wedge \text{MemberOf}(x, \text{Balls}) \Rightarrow \text{MemberOf}(x, \text{BasketBalls}))$
- A category as a whole has some properties
  - $\text{MemberOf}(\text{Dogs}, \text{DomesticatedSpecies})$



# Relations between categories

- Two or more categories are **disjoint** if they have no members in common:
  - $\text{Disjoint}(s) \Leftrightarrow (\forall c_1, c_2 \ c_1 \in s \wedge c_2 \in s \wedge c_1 \neq c_2 \Rightarrow \text{Intersection}(c_1, c_2) = \{\})$
  - Example;  $\text{Disjoint}(\{\text{animals, vegetables}\})$
- A set of categories  $s$  constitutes an **exhaustive decomposition** of a category  $c$  if all members of the set  $c$  are covered by categories in  $s$ :
  - $\text{E.D.}(s, c) \Leftrightarrow (\forall i: i \in c \Rightarrow \exists c_2: c_2 \in s \wedge i \in c_2)$
  - Example:  $\text{ExhaustiveDecomposition}(\{\text{Americans, Canadians, Mexicans}\}, \text{NorthAmericans})$ .



# Relations between categories

- A ***partition*** is a disjoint exhaustive decomposition:
  - $\text{Partition}(s,c) \Leftrightarrow \text{Disjoint}(s) \wedge \text{E.D.}(s,c)$
  - Example:  $\text{Partition}(\{\text{Males}, \text{Females}\}, \text{Persons})$ .
- Is  $(\{\text{Americans}, \text{Canadians}, \text{Mexicans}\}, \text{NorthAmericans})$  a partition?
- Categories can be defined by providing necessary and sufficient conditions for membership
  - $\forall x \text{ Bachelor}(x) \Leftrightarrow \text{Male}(x) \wedge \text{Adult}(x) \wedge \text{Unmarried}(x)$



## Natural kinds

- Many categories have no clear-cut definitions (chair, bush, book).
- Tomatoes: sometimes green, red, yellow, black. Mostly round.
- One solution: category *Typical(Tomatoes)*.
  - $\forall x: x \in \text{Typical}(\text{Tomatoes}) \Rightarrow \text{Red}(x) \wedge \text{Spherical}(x)$ .
  - We can write down useful facts about categories without providing exact definitions.
- What about “bachelor”? Quine challenged the utility of the notion of *strict definition*. We might question a statement such as “the Pope is a bachelor”.



# Physical composition

- One object may be part of another:
  - PartOf(Bucharest,Romania)
  - PartOf(Romania,EasternEurope)
  - PartOf(EasternEurope,Europe)
- The PartOf predicate is transitive (and irreflexive), so we can infer that PartOf(Bucharest,Europe)
- More generally:
  - $\forall x \text{ PartOf}(x,x)$
  - $\forall x,y,z \text{ PartOf}(x,y) \wedge \text{PartOf}(y,z) \Rightarrow \text{PartOf}(x,z)$
- Often characterized by structural relations among parts.
  - E.g. Biped(a)  $\Rightarrow$   
 $(\exists l_1, l_2, b)(\text{Leg}(l_1) \wedge \text{Leg}(l_2) \wedge \text{Body}(b) \wedge$   
 $\text{PartOf}(l_1, a) \wedge \text{PartOf}(l_2, a) \wedge \text{PartOf}(b, a) \wedge$   
 $\text{Attached}(l_1, b) \wedge \text{Attached}(l_2, b) \wedge$   
 $l_1 \neq l_2 \wedge (\forall l_3)(\text{Leg}(l_3) \Rightarrow (l_3 = l_1 \vee l_3 = l_2)))$

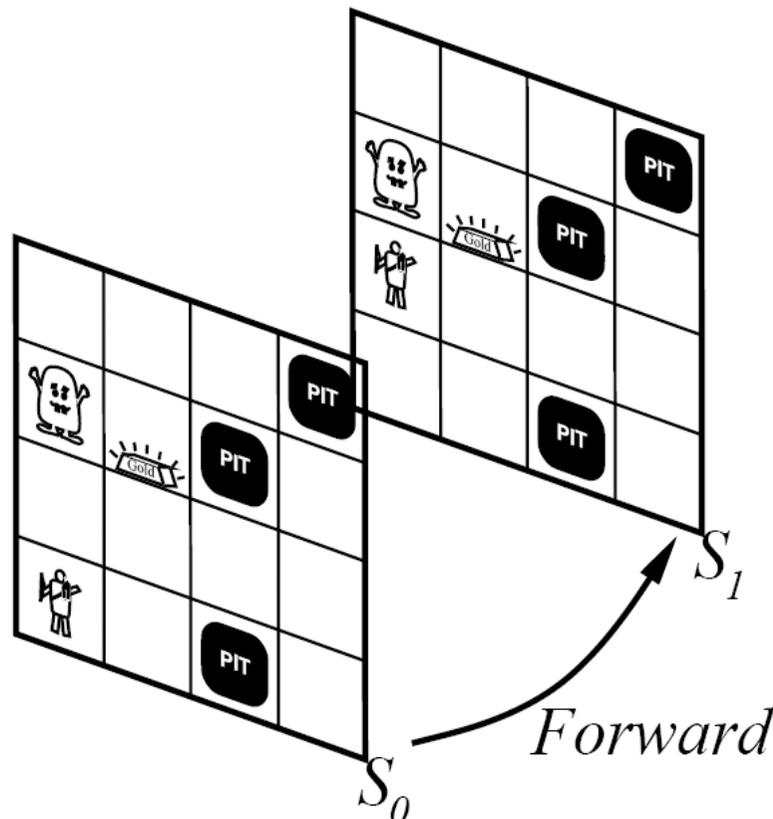


# Measurements

- Objects have height, mass, cost, ....  
Values that we assign to these are **measures**
- Combine Unit functions with a number:  $\text{Length}(L_1) = \text{Inches}(1.5) = \text{Centimeters}(3.81)$ .
- Conversion between units:  
 $\forall i \text{ Centimeters}(2.54 \times i) = \text{Inches}(i)$ .
- Some measures have no scale: Beauty, Difficulty, etc.
  - Most important aspect of measures: is that they are orderable.
  - Don't care about the actual numbers. (An apple can have deliciousness .9 or .1.)



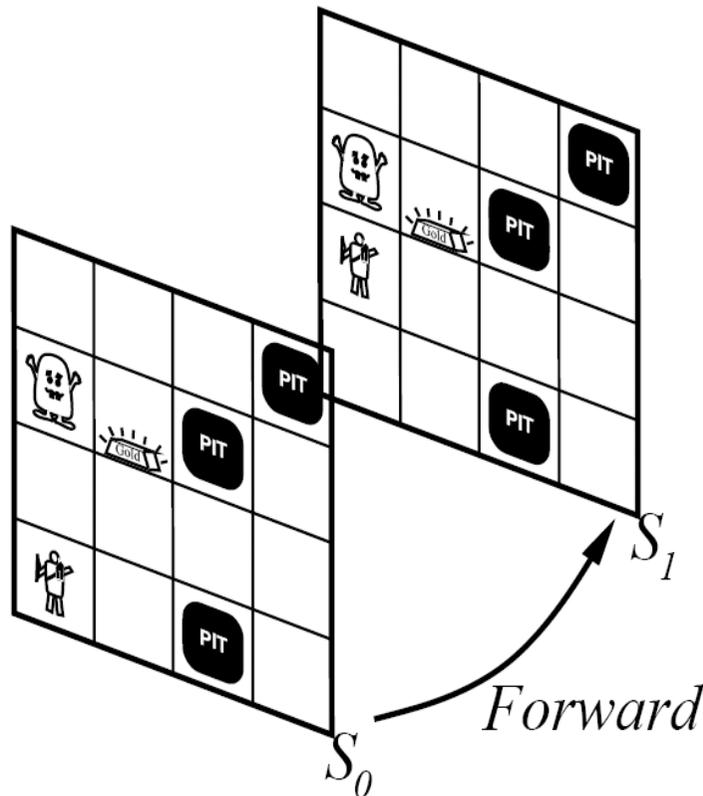
# Actions, events and situations



- Reasoning about outcome of actions is central to KB-agent.
- How can we keep track of location in FOL?
  - Remember the multiple copies in PL.
- Representing time by situations (states resulting from the execution of actions).
  - Situation calculus



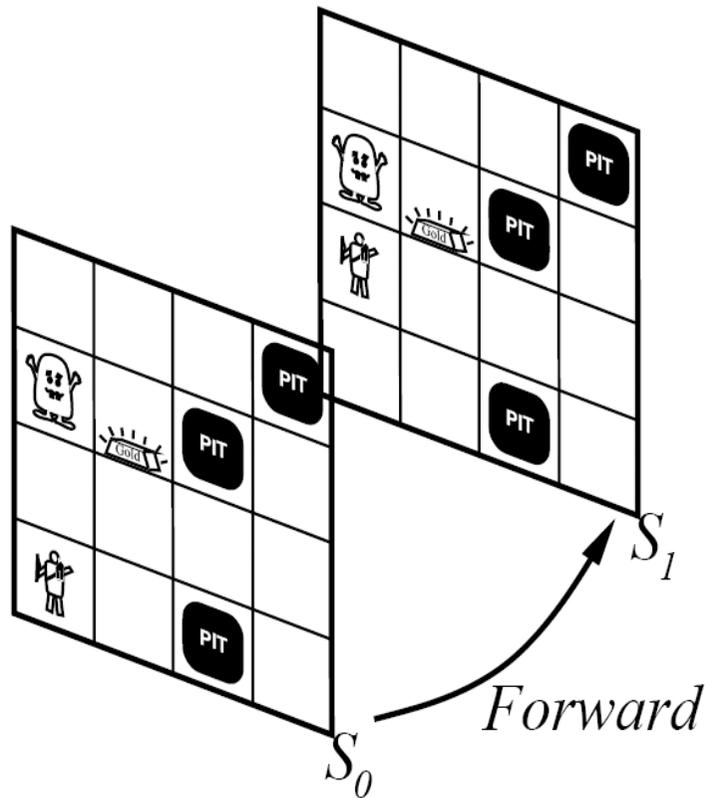
# Actions, events and situations



- Situation calculus:
  - Actions are logical terms
  - Situations are logical terms consisting of
    - The initial situation  $I$
    - All situations resulting from the action on  $I$  ( $=Result(a,s)$ )
  - Fluents are functions and predicates that vary from one situation to the next.
    - E.g.  $\neg Holding(G_1, S_0)$
  - Eternal predicates are also allowed
    - E.g.  $Gold(G_1)$



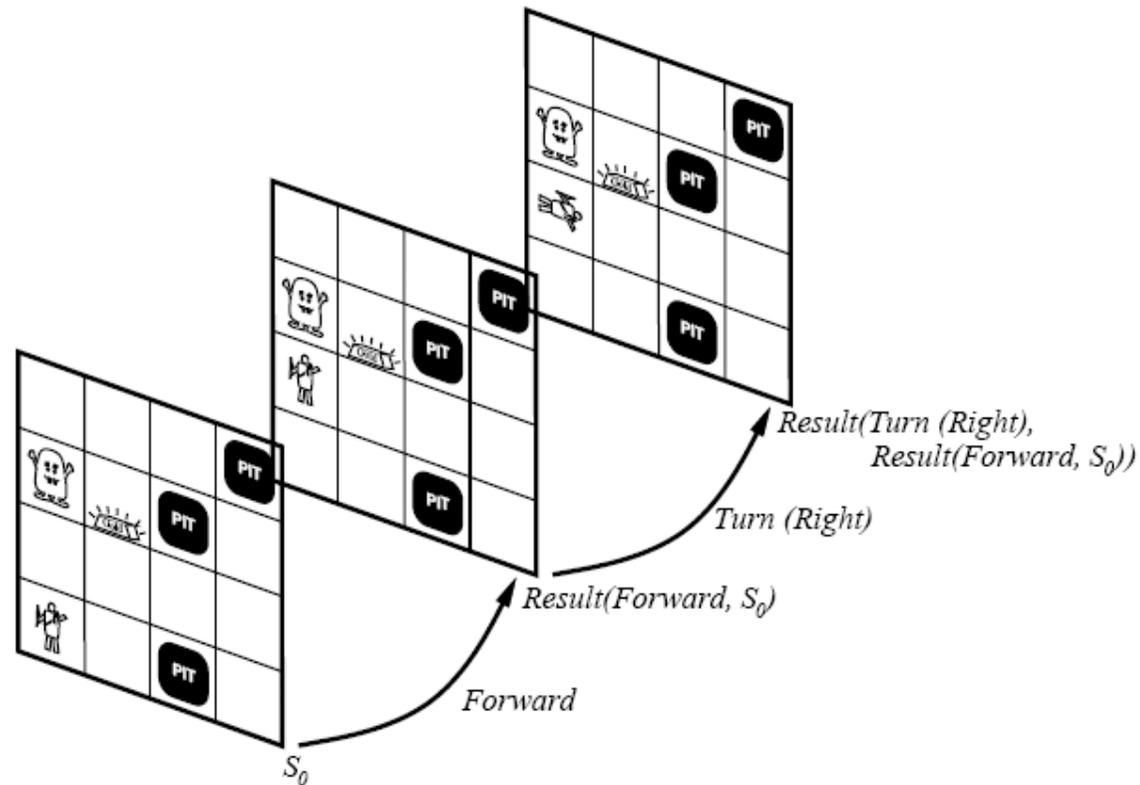
# Actions, events and situations



- Results of action sequences are determined by the individual actions.
- *Projection task*: an SC agent should be able to deduce the outcome of a sequence of actions.
- *Planning task*: find a sequence that achieves a desirable effect



# Actions, events and situations



# Describing change

- Simple Situation calculus requires two axioms to describe change:

- Possibility axiom: when is it possible to do the action

$$At(Agent, x, s) \wedge Adjacent(x, y) \Rightarrow Poss(Go(x, y), s)$$

- Effect axiom: describe changes due to action

$$Poss(Go(x, y), s) \Rightarrow At(Agent, y, Result(Go(x, y), s))$$

- What stays the same?

- Frame problem: how to represent all things that stay the same?

- Frame axiom: describe non-changes due to actions

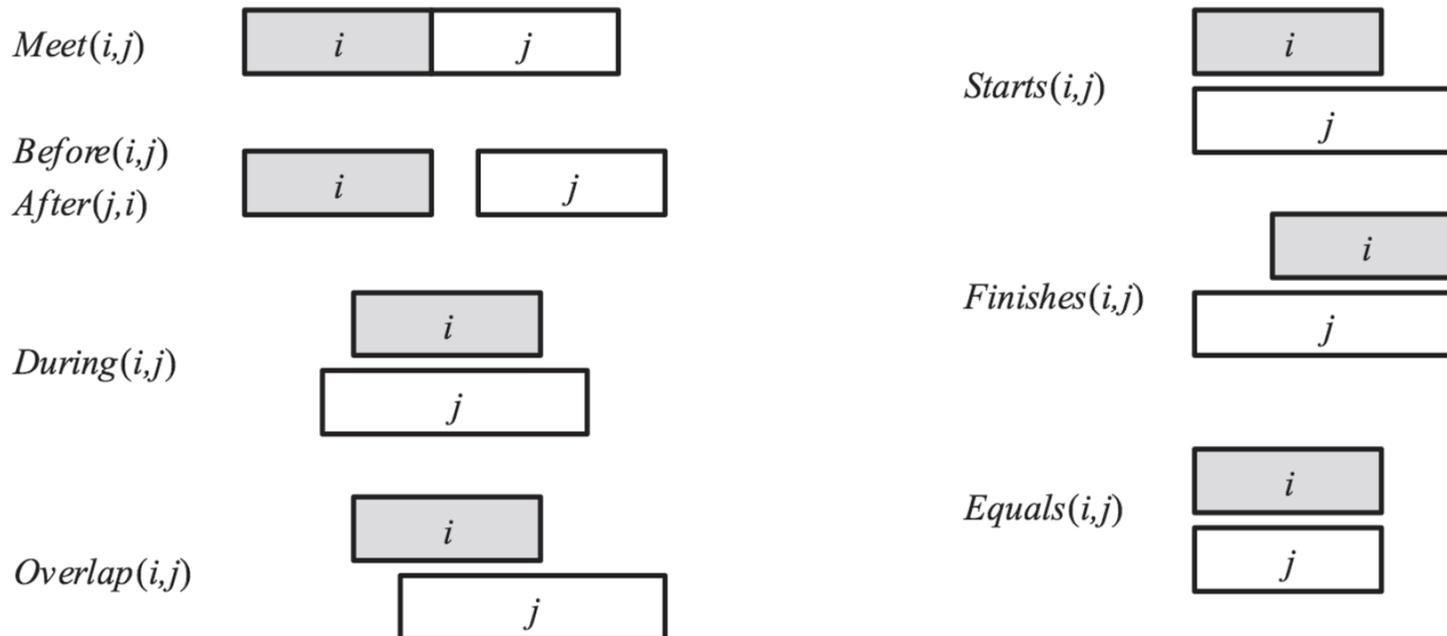
$$At(o, x, s) \wedge (o \neq Agent) \wedge \neg Holding(o, s) \Rightarrow At(o, x, Result(Go(y, z), s))$$



# Time relations and time logic

- To overcome limitations in the situation calculus, event calculus can be used.
  - E.g. predicate *HoldsAt* (*fluent*, *time*) describes that a specific sentence *f* is true at time *t*.

Time relations can be as follows:



# Representational frame problem

- If there are  $F$  fluents and  $A$  actions then we need  $AF$  frame axioms to describe other objects are stationary unless they are held.
  - We write down the effect of each actions
- Solution; describe how each fluent changes over time
  - Successor-state axiom:
$$Pos(a,s) \Rightarrow (At(Agent,y,Result(a,s)) \Leftrightarrow (a = Go(x,y)) \vee (At(Agent,y,s) \wedge a \neq Go(y,z)))$$
  - Note that next state is completely specified by current state.
  - Each action effect is mentioned only once.



## Other problems

- How to deal with secondary (implicit) effects?
  - If the agent is carrying the gold and the agent moves then the gold moves too.
  - Ramification problem
- How to decide EFFICIENTLY whether fluents hold in the future?
  - Inferential frame problem.
- Extensions:
  - Event calculus (when actions have a duration)
  - Process categories



# Mental events and objects

- So far, KB agents can have beliefs and deduce new beliefs
- What about knowledge about beliefs? What about knowledge about the inference process?
  - Requires a model of the mental objects in someone's head and the processes that manipulate these objects.
- Relationships between agents and mental objects: believes, knows, wants, ...
  - Believes(Lois,Flies(Superman)) with Flies(Superman) being a function ... a candidate for a mental object (reification).
  - Agent can now reason about the beliefs of agents.



# The internet shopping world

- A Knowledge Engineering example
- An agent that helps a buyer to find product offers on the internet.
  - IN = product description (precise or  $\neg$ precise)
  - OUT = list of webpages that offer the product for sale.
- Environment = WWW
- Percepts = web pages (character strings)
  - Extracting useful information required.



# The internet shopping world

- Find relevant product offers

$$\text{RelevantOffer}(\text{page}, \text{url}, \text{query}) \Leftrightarrow \text{Relevant}(\text{page}, \text{url}, \text{query}) \wedge \text{Offer}(\text{page})$$

- Write axioms to define Offer(x)
- Find relevant pages: Relevant(x,y,z) ?
  - Start from an initial set of stores.
  - What is a relevant category?
  - What are relevant connected pages?
- Require rich category vocabulary.
  - Synonymy and ambiguity
- How to retrieve pages: *GetPage(url)*?
  - Procedural attachment

- Compare offers (information extraction).



# Reasoning systems for categories

- How to organise and reason with categories?
  - Semantic networks
    - Visualize knowledge-base
    - Efficient algorithms for category membership inference
  - Description logics
    - Formal language for constructing and combining category definitions
    - Efficient algorithms to decide subset and superset relationships between categories.



# Description logics

- Are designed to describe definitions and properties about categories
  - A formalization of semantic networks
- Principal inference task is
  - *Subsumption*: checking if one category is the subset of another by comparing their definitions
  - *Classification*: checking whether an object belongs to a category.
  - Consistency: whether the category membership criteria are logically satisfiable.



# Reasoning with Default Information

- “The following courses are offered: CS101, CS102, CS106, EE101”
  - Four (data base semantics)
    - Assume that this information is complete (not asserted ground atomic sentences are false)  
= CLOSED WORLD ASSUMPTION
    - Assume that distinct names refer to distinct objects  
= UNIQUE NAMES ASSUMPTION
  - Between one and infinity (logic)
    - Does not make these assumptions
    - Requires completion.



# Truth maintenance systems

- Many of the inferences have default status rather than being absolutely certain
  - Inferred facts can be wrong and need to be retracted = BELIEF REVISION.
  - Assume KB contains sentence  $P$  and we want to execute  $\text{TELL}(\text{KB}, \neg P)$ 
    - To avoid contradiction:  $\text{RETRACT}(\text{KB}, P)$
    - But what about sentences inferred from  $P$ ?
- Truth maintenance systems are designed to handle these complications.



# Summary

- Knowledge representation is crucial for efficient reasoning
- Ontologies are a widely used way for representing knowledge
- Upper ontology to describe main concepts and object classes of the world
- Individual ontologies for specific domains needed
- Different ways of reasoning
  - Navigation in semantic networks
  - Formal reasoning using logical representations
- Problem: Handling of default values

