

Vorlesung

Grundlagen der

Künstlichen Intelligenz

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Chapter 10 cont'd (3rd ed.) + 11

Classical Planning, Planning in the Real World

From the last session

- General description of plans and planning algorithms
- Planning as search for goal states
- GraphPlan algorithm



The GRAPHPLAN Algorithm

- How to extract a solution directly from the PG

function GRAPHPLAN(*problem*) **return** *solution* or failure

graph ← INITIAL-PLANNING-GRAPH(*problem*)

goals ← GOALS[*problem*]

loop do

if *goals* all non-mutex in last level of graph **then do**

solution ← EXTRACT-SOLUTION(*graph*, *goals*,
LENGTH(*graph*))

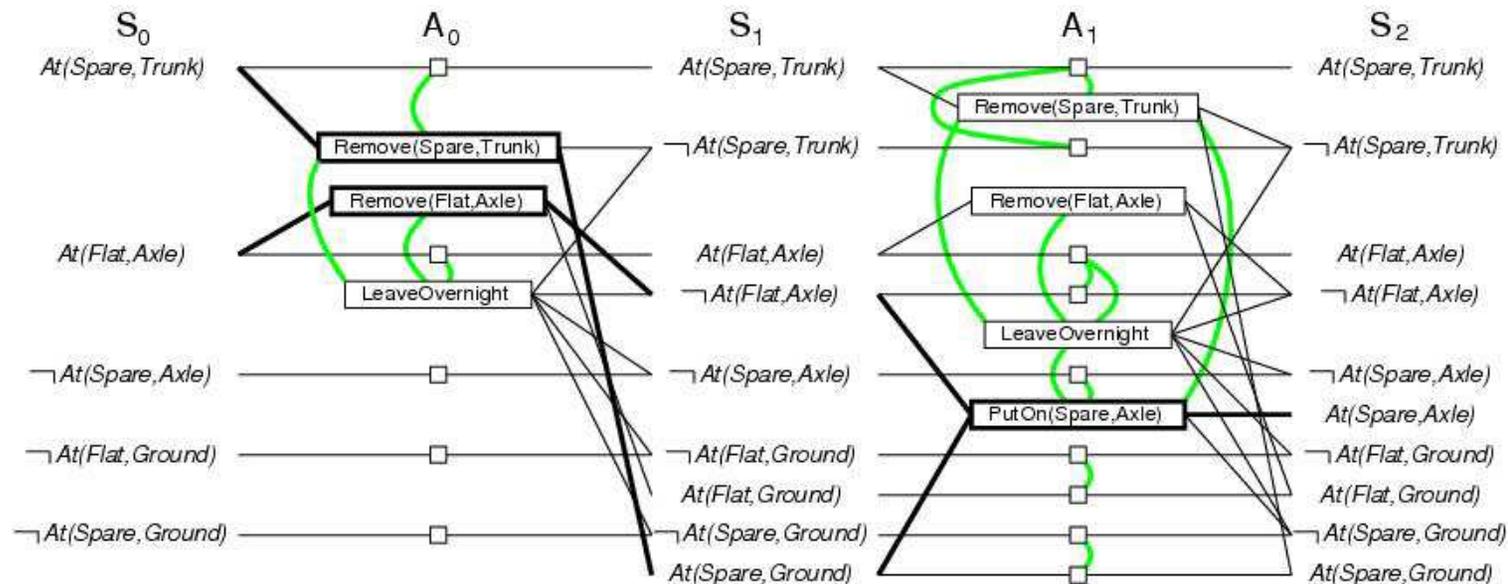
if *solution* ≠ failure **then return** *solution*

else if NO-SOLUTION-POSSIBLE(*graph*) **then return** failure

graph ← EXPAND-GRAPH(*graph*, *problem*)



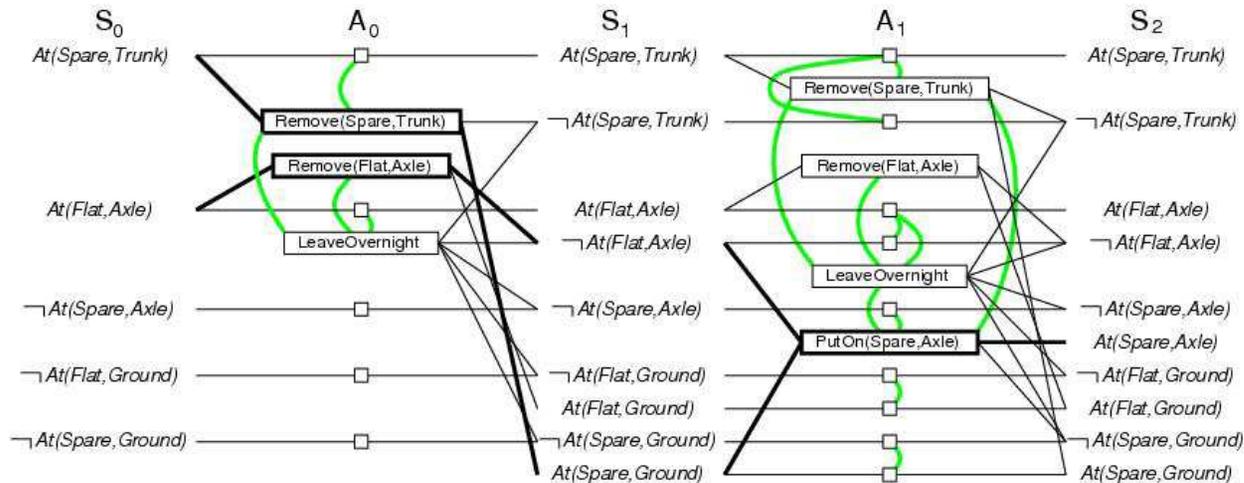
GRAPHPLAN example



- Initially the plan consist of 5 literals from the initial state and the literals resulting from the closed-world-assumption (CWA) (S0).
- Add actions whose preconditions are satisfied by EXPAND-GRAPH (A0)
- Also add persistence actions and mutex relations.
- Add the effects at level S1
- Repeat until goal is in level Si



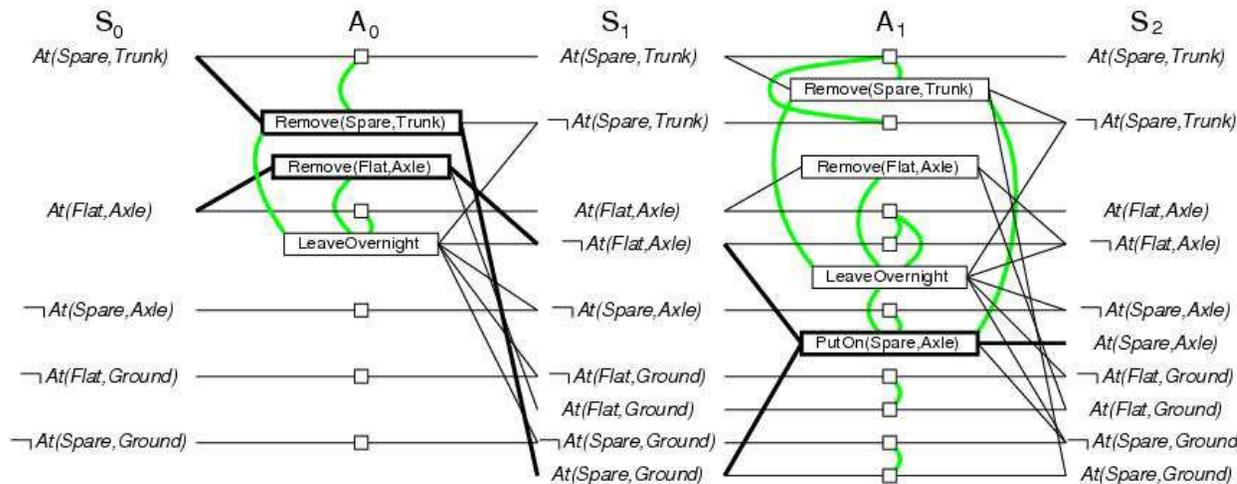
GRAPHPLAN example



- EXPAND-GRAPH also looks for mutex relations
 - Inconsistent effects
 - E.g. $Remove(Spare, Trunk)$ and $LeaveOverNight$
 - Interference
 - E.g. $Remove(Flat, Axle)$ and $LeaveOverNight$
 - Competing needs
 - E.g. $PutOn(Spare, Axle)$ and $Remove(Flat, Axle)$
 - Inconsistent support
 - E.g. in S_2 , $At(Spare, Axle)$ and $At(Flat, Axle)$



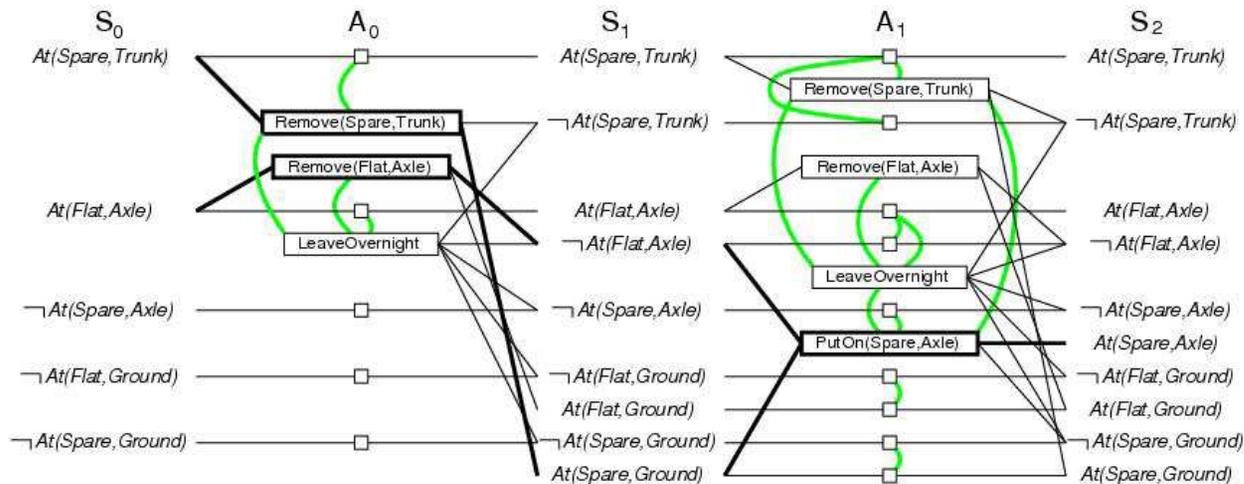
GRAPHPLAN example



- In S2, the goal literal exists and is not mutex with any other
 - Solution might exist and EXTRACT-SOLUTION will try to find it
- EXTRACT-SOLUTION can use Boolean CSP to solve the problem or a search process:
 - Initial state = last level of PG and goal goals of planning problem
 - Actions = select any set of non-conflicting actions that cover the goals in the state
 - Goal = reach level S0 such that all goals are satisfied
 - Cost = 1 for each action.



GRAPHPLAN example



- Termination? YES
- PG are monotonically increasing or decreasing:
 - Literals increase monotonically
 - Actions increase monotonically
 - Mutexes decrease monotonically
- Because of these properties and because there is a finite number of actions and literals, every PG will eventually level off !



Planning with propositional logic

- Planning can be done by proving theorem in situation calculus.
- Here: test the *satisfiability* of a logical sentence:

initial state \wedge *all possible action descriptions* \wedge *goal*

- Sentence contains propositions for every action occurrence.
 - A model will assign true to the actions that are part of the correct plan and false to the others
 - An assignment that corresponds to an incorrect plan will not be a model because of inconsistency with the assertion that the goal is true.
 - If the planning is unsolvable the sentence will be unsatisfiable.



SATPLAN algorithm

function SATPLAN(*problem*, T_{max}) **return** *solution* or failure

inputs: *problem*, a planning problem

T_{max} , an upper limit to the plan length

for $T=0$ **to** T_{max} **do**

cnf, *mapping* \leftarrow TRANSLATE-TO_SAT(*problem*, T)

assignment \leftarrow SAT-SOLVER(*cnf*)

if *assignment* is not null **then**

return EXTRACT-SOLUTION(*assignment*, *mapping*)

return failure



cnf, mapping ← TRANSLATE-TO_SAT(*problem, T*)

- Distinct propositions for assertions about each time step.
 - Superscripts denote the time step
 $At(P1,SFO)^0 \wedge At(P2,JFK)^0$
 - No CWA thus specify which propositions are not true
 $\neg At(P1,SFO)^0 \wedge \neg At(P2,JFK)^0$
 - Unknown propositions are left unspecified.
- The goal is associated with a particular time-step
 - But which one?



cnf, mapping \leftarrow TRANSLATE-TO_SAT(*problem, T*)

- How to determine the time step where the goal will be reached?
 - Start at $T=0$
 - Assert $At(P1, SFO)^0 \wedge At(P2, JFK)^0$
 - Failure .. Try $T=1$
 - Assert $At(P1, SFO)^1 \wedge At(P2, JFK)^1$
 - ...
 - Repeat this until some minimal path length is reached.
 - Termination is ensured by T_{max}



cnf, mapping ← TRANSLATE-TO_SAT(*problem, T*)

- How to encode actions into PL?

- Propositional versions of successor-state axioms

$$At(P1, JFK)^1 \Leftrightarrow$$

$$(At(P1, JFK)^0 \wedge \neg(Fly(P1, JFK, SFO)^0 \wedge At(P1, JFK)^0)) \vee \\ (Fly(P1, SFO, JFK)^0 \wedge At(P1, SFO)^0)$$

- Such an axiom is required for each plane, airport and time step
- If more airports add another way to travel than additional disjuncts are required

- Once all these axioms are in place, the satisfiability algorithm can start to find a plan.



assignment ← SAT-SOLVER(*cnf*)

- Multiple models can be found
- They are NOT satisfactory: (for $T=1$)
 $Fly(P1, SFO, JFK)^0 \wedge Fly(P1, JFK, SFO)^0 \wedge Fly(P2, JFK, SFO)^0$
The second action is infeasible
Yet the plan IS a model of the sentence

initial state \wedge *all possible action descriptions* \wedge *goal*¹

- Avoiding illegal actions: pre-condition axioms

$$Fly(P1, SFO, JFK)^0 \Rightarrow At(P1, JFK)$$

- Exactly one model now satisfies all the axioms where the goal is achieved at $T=1$.



assignment ← SAT-SOLVER(*cnf*)

- A plane can fly at two destinations at once
- They are NOT satisfactory: (for T=1)
 $Fly(P1, SFO, JFK)^0 \wedge Fly(P2, JFK, SFO)^0 \wedge Fly(P2, JFK, LAX)^0$
The second action is infeasible
Yet the plan allows spurious relations
- Avoid spurious solutions: action-exclusion axioms
 $\neg(Fly(P2, JFK, SFO)^0 \wedge Fly(P2, JFK, LAX))$
Prevents simultaneous actions
- Lost of flexibility since plan becomes totally ordered : no actions are allowed to occur at the same time.
 - Restrict exclusion to preconditions



Planning in the Real World

Until now: planning considered as search for goal states

In real-world applications, additional constraints apply

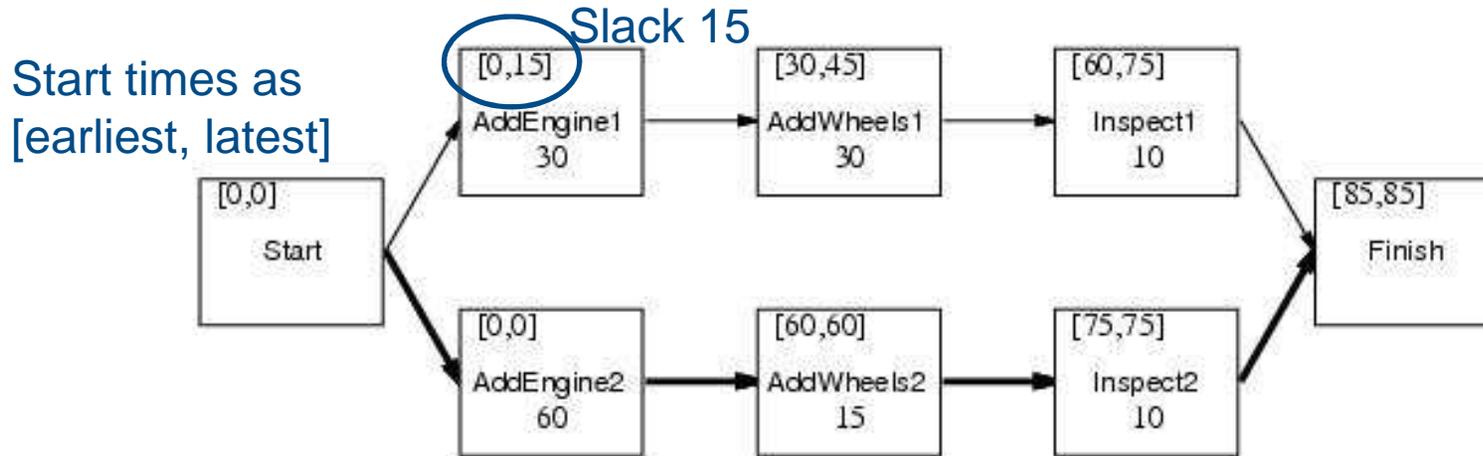
- Time
 - Execution times are relevant, especially in concurrent plans

- Resources
 - Availability of reusable resources, e.g. machines, robots, ...
 - Availability of consumable resources, e.g. fuel, screws, ...

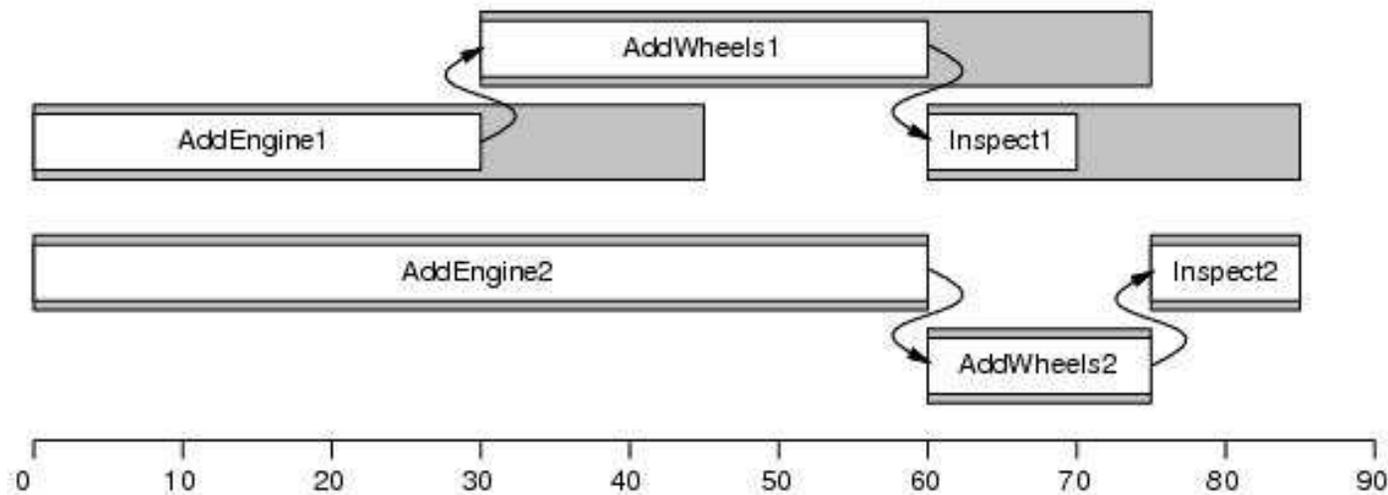
- In addition to finding a valid plan, **scheduling** is important
 - Execution order in concurrent plans determines overall execution time



Scheduling example – critical path method



Bold arrows: critical path, i.e. maximal duration, actions with slack zero



Scheduling example – critical path method

- Example with limited resources
 - Only 1 engine hoist leads to sequentialisation of AddEngine



Hierarchical planning

- Several levels of abstraction for the plans
- Detailing out the plan during the planning steps, can be deferred to plan execution phase for the sake of flexibility
 - Off-line vs. on-line planning
 - E.g. in driving, route with cities planned off-line, exact steering parameters on-line based on sensor information
- Plan refinement
 - Simplest form: Description as tuple

(original plan, refined plan)



Hierarchical planning

Plan refinement example

- List of possible substitutions
(start and termination conditions not shown)

$((transport), (road - transport))$

$((transport), (road - transport, railroad - transport, road - transport))$

$((transport), (road - transport, sea - Transport, road - transport))$

$((transport), (road - transport, railroad - transport, sea - transport, road - transport))$

$((transport), (road - transport, air - transport, road - transport))$

- Choice of actual substitutions needs semantic information
- Choice can be restricted by pre-conditions



Hierarchical planning

Plan refinement example with resource limitations

- Move object on table
- Resources are 1 mobile manipulator, 1 mobile base
- Abstract operation move can be re-written as

$((move), (attach, push))$	mobile base
$((move), (grasp, pull))$	mobile manipulator

- The mobile manipulator can perform both alternatives, the mobile base only the first



Hierarchical planning

Plan refinement example with resource limitations

- Refinement of move operation

$((move), (push))$

$((move), (attach, push))$

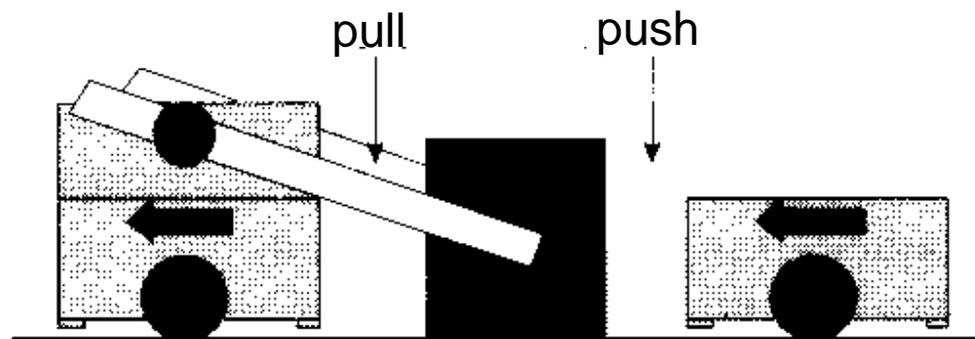
$((move), (approach, attach, push))$

alternatively stepwise refinement

$((move), (push))$

$((push), (attach, push))$

$((attach), (approach, attach))$



Hierarchical planning

Plan refinement example with resource limitations

- Formal description of the refinement by replace operator

$replace(original, substitute, precondition, additional_property)$

- In the example (off-line variant)

$$replace \left(\begin{array}{l} (move), \\ (grasp(manipulator), pull(manipulator)), \\ (available(manipulator)), \\ (addcost(rentalfee)) \end{array} \right)$$


Hierarchical planning

Plan refinement example with resource limitations

- On-line variant with dynamic resource allocation during run-time:

$$\text{replace} \left(\begin{array}{c} (move), \\ (\text{request}(manipulator), \text{grasp}(manipulator), \text{pull}(manipulator)), \\ (\text{own}(rentalfee)), \\ (\text{consumed}(rentalfee), \text{addcost}(rentalfee)) \end{array} \right)$$



Additional aspects of planning

Not considered in the context of this course

- Single vs. multi agent plans
- Centralized vs. decentralized planning
- Plan coordination
- Fault-tolerance aspects
 - Concurrent alternatives
 - Plan repair techniques
- Motion planning techniques
 - See module IN2138 Robot Motion Planning



Summary

- Planning is an area of great interest within AI
- Biggest problem is the combinatorial explosion in states.

- Planning described as set of preconditions, actions, and postconditions
- Use of search strategies to create plans
- Use of theorem proving

- Consideration of limited resources and time

- Hierarchical planning approaches



Evaluation

Please fill in the evaluation forms



